Microphones, ground fault circuit interrupters, seismographs, and read/write heads for computer drives and tape recorders are applications of electromagnetic induction.

[\*A changing current in a coil of wire will produce a changing magnetic field that induces an emf in a second coil placed nearby. The mutual inductance, M, is defined by

$$\mathscr{E}_2 = -M \frac{\Delta I_1}{\Delta t}.$$
 (21-8)

[\*Within a single coil, the changing B due to a changing current induces an opposing emf, &, so a coil has a self-inductance L defined by

$$\mathscr{E} = -L \frac{\Delta I}{\Delta t}.$$
 (21–9)

[\*The energy stored in an inductance L carrying current I is given by  $U = \frac{1}{2}LI^2$ . This energy can be thought of as being stored in the magnetic field of the inductor. The energy density u in any magnetic field B is given by

$$u = \frac{1}{2} \frac{B^2}{\mu_0}.$$
 (21–10)]

[\*When an inductance L and resistor R are connected in series to a source of emf, V, the current rises as

$$I = \frac{V}{R} (1 - e^{-t/\tau}),$$

where  $\tau = L/R$  is the time constant. If the battery is suddenly switched out of the LR circuit, the current drops exponentially,  $I = I_{\text{max}} e^{-t/\tau}$ .]

[\*Inductive and capacitive reactance, X, defined as for resistors, is the proportionality constant between voltage and current (either the rms or peak values). Across an inductor,

$$V = IX_L, (21-11a)$$

and across a capacitor,

$$V = IX_C. (21-12a)$$

The reactance of an inductor increases with frequency

$$X_L = 2\pi f L, (21-11b)$$

whereas the reactance of a capacitor decreases with frequency f,

$$X_C = \frac{1}{2\pi f C}$$
 (21–12b)

The current through a resistor is always in phase with the voltage across it, but in an inductor, the current lags the voltage by 90°, and in a capacitor the current leads the voltage by 90°.

[\*In an LRC series circuit, the total impedance Z is defined by the equivalent of V = IR for resistance, namely,

$$V_0 = I_0 Z$$
 or  $V_{\text{rms}} = I_{\text{rms}} Z$ ; (21-14)

Z is given by

$$V_0 = I_0 Z$$
 or  $V_{\text{rms}} = I_{\text{rms}} Z;$  (21-14)  
 $Z = \sqrt{R^2 + (X_L - X_C)^2}.$  (21-15a)

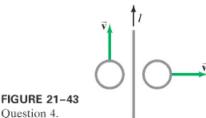
[\*An LRC series circuit resonates at a frequency given by

$$f_0 = \frac{1}{2\pi} \sqrt{\frac{1}{LC}}.$$
 (21–19)

The rms current in the circuit is largest when the applied voltage has a frequency equal to  $f_0$ .

## Questions

- 1. What would be the advantage, in Faraday's experiments (Fig. 21-1), of using coils with many turns?
- 2. What is the difference between magnetic flux and magnetic field?
- 3. Suppose you are holding a circular ring of wire and suddenly thrust a magnet, south pole first, away from you toward the center of the circle. Is a current induced in the wire? Is a current induced when the magnet is held steady within the ring? Is a current induced when you withdraw the magnet? In each case, if your answer is yes, specify the direction.
- 4. Two loops of wire are moving in the vicinity of a very long straight wire carrying a steady current as shown in Fig. 21-43. Find the direction of the induced current in each loop.



5. Suppose you are looking along a line through the centers of two circular (but separate) wire loops, one behind the other. A battery is suddenly connected to the front loop, establishing a clockwise current. (a) Will a current be induced in the second loop? (b) If so, when does this current start? (c) When does it stop? (d) In what direction is this current? (e) Is there a force between the two loops? (f) If so, in what direction?

6. In Fig. 21-44, determine the direction of the induced current in resistor RA when (a) coil B is moved toward coil A, (b) when coil B is moved away from A, (c) when the resistance  $R_{\rm B}$  is increased.

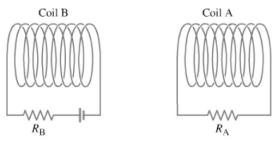


FIGURE 21-44 Question 6.

- 7. In situations where a small signal must travel over a distance, a "shielded cable" is used in which the signal wire is surrounded by an insulator and then enclosed by a cylindrical conductor carrying the return current. Why is a "shield" necessary?
- 8. What is the advantage of placing the two insulated electric wires carrying ac close together or even twisted about each other?
- \*9. Explain why, exactly, the lights may dim briefly when a refrigerator motor starts up. When an electric heater is turned on, the lights may stay dimmed as long as the heater is on. Explain the difference.