

The **kinetic energy** of a particle of mass  $m$  moving with a speed  $v$  (where  $v$  is small compared with the speed of light) is

$$K \equiv \frac{1}{2}mv^2 \quad (7.14)$$

The **work–kinetic energy theorem** states that the net work done on a particle by external forces equals the change in kinetic energy of the particle:

$$\sum W = K_f - K_i = \frac{1}{2}mv_f^2 - \frac{1}{2}mv_i^2 \quad (7.16)$$

If a frictional force acts, then the work–kinetic energy theorem can be modified to give

$$K_i + \sum W_{\text{other}} - f_k d = K_f \quad (7.17b)$$

The **instantaneous power**  $\mathcal{P}$  is defined as the time rate of energy transfer. If an agent applies a force  $\mathbf{F}$  to an object moving with a velocity  $\mathbf{v}$ , the power delivered by that agent is

$$\mathcal{P} \equiv \frac{dW}{dt} = \mathbf{F} \cdot \mathbf{v} \quad (7.18)$$

## QUESTIONS

- Consider a tug-of-war in which two teams pulling on a rope are evenly matched so that no motion takes place. Assume that the rope does not stretch. Is work done on the rope? On the pullers? On the ground? Is work done on anything?
- For what values of  $\theta$  is the scalar product (a) positive and (b) negative?
- As the load on a spring hung vertically is increased, one would not expect the  $F_s$ -versus- $x$  curve to always remain linear, as shown in Figure 7.10d. Explain qualitatively what you would expect for this curve as  $m$  is increased.
- Can the kinetic energy of an object be negative? Explain.
- (a) If the speed of a particle is doubled, what happens to its kinetic energy? (b) If the net work done on a particle is zero, what can be said about the speed?
- In Example 7.16, does the required power increase or decrease as the force of friction is reduced?
- An automobile sales representative claims that a “souped-up” 300-hp engine is a necessary option in a compact car (instead of a conventional 130-hp engine). Suppose you intend to drive the car within speed limits ( $\leq 55$  mi/h) and on flat terrain. How would you counter this sales pitch?
- One bullet has twice the mass of another bullet. If both bullets are fired so that they have the same speed, which has the greater kinetic energy? What is the ratio of the kinetic energies of the two bullets?
- When a punter kicks a football, is he doing any work on the ball while his toe is in contact with it? Is he doing any work on the ball after it loses contact with his toe? Are any forces doing work on the ball while it is in flight?
- Discuss the work done by a pitcher throwing a baseball. What is the approximate distance through which the force acts as the ball is thrown?
- Two sharpshooters fire 0.30-caliber rifles using identical shells. The barrel of rifle A is 2.00 cm longer than that of rifle B. Which rifle will have the higher muzzle speed? (*Hint:* The force of the expanding gases in the barrel accelerates the bullets.)
- As a simple pendulum swings back and forth, the forces acting on the suspended mass are the force of gravity, the tension in the supporting cord, and air resistance. (a) Which of these forces, if any, does no work on the pendulum? (b) Which of these forces does negative work at all times during its motion? (c) Describe the work done by the force of gravity while the pendulum is swinging.
- The kinetic energy of an object depends on the frame of reference in which its motion is measured. Give an example to illustrate this point.
- An older model car accelerates from 0 to a speed  $v$  in 10 s. A newer, more powerful sports car accelerates from 0 to  $2v$  in the same time period. What is the ratio of powers expended by the two cars? Consider the energy coming from the engines to appear only as kinetic energy of the cars.