

EXAMPLE 19-5 **Current in one branch.** What is the current through the 500- Ω resistor in Fig. 19-8a?

APPROACH We need to find the voltage across the 500- Ω resistor, which is the voltage between points b and c in Fig. 19-8a, and we call it V_{bc} . Once V_{bc} is known, we can apply Ohm's law, $V = IR$, to get the current. First we find the voltage across the 400- Ω resistor, V_{ab} , since we know that 17 mA passes through it.

SOLUTION V_{ab} can be found using $V = IR$:

$$V_{ab} = (0.0174 \text{ A})(400 \Omega) = 7.0 \text{ V.}$$

Since the total voltage across the network of resistors is $V_{ac} = 12.0 \text{ V}$, then V_{bc} must be $12.0 \text{ V} - 7.0 \text{ V} = 5.0 \text{ V}$. Then Ohm's law applied to the 500- Ω resistor tells us that the current I_1 through that resistor is

$$I_1 = \frac{5.0 \text{ V}}{500 \Omega} = 1.0 \times 10^{-2} \text{ A} = 10 \text{ mA.}$$

This is the answer we wanted. We can also calculate the current I_2 through the 700- Ω resistor since the voltage across it is also 5.0 V:

$$I_2 = \frac{5.0 \text{ V}}{700 \Omega} = 7 \text{ mA.}$$

NOTE When I_1 combines with I_2 to form the total current I (at point c in Fig. 19-8a), their sum is $10 \text{ mA} + 7 \text{ mA} = 17 \text{ mA}$. This is, of course, the total current I as calculated in Example 19-4.

CONCEPTUAL EXAMPLE 19-6 **Bulb brightness in a circuit.** The circuit shown in Fig. 19-9 has three identical lightbulbs, each of resistance R . (a) When switch S is closed, how will the brightness of bulbs A and B compare with that of bulb C? (b) What happens when switch S is opened? Use a minimum of mathematics in your answers.

RESPONSE (a) With switch S closed, the current that passes through bulb C must split into two equal parts when it reaches the junction leading to bulbs A and B. It splits into equal parts because the resistance of bulb A equals that of B. Thus, bulbs A and B each receive half of C's current; A and B will be equally bright, but they will be less bright than bulb C.

(b) When the switch S is open, no current can flow through bulb A, so it will be dark. We now have a simple one-loop series circuit, and we expect bulbs B and C to be equally bright. However, the equivalent resistance of this circuit ($= R + R$) is greater than that of the circuit with the switch closed. When we open the switch, we increase the resistance and reduce the current leaving the battery. Thus, bulb C will dim when we open the switch. Bulb B gets more current when the switch is open (you may have to use some mathematics here), and so it will be brighter than with the switch closed, and B will be as bright as C.

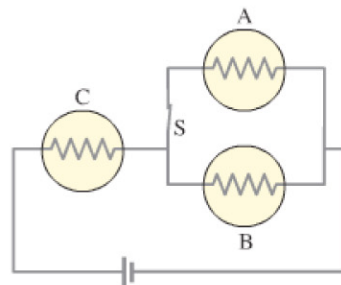


FIGURE 19-9 Example 19-6, three identical lightbulbs. Each yellow circle with \sim inside represents a lightbulb and its resistance.