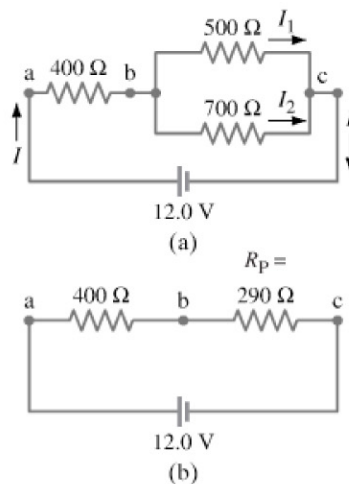


FIGURE 19–8 (a) Circuit for Examples 19–4 and 19–5. (b) Equivalent circuit, showing the equivalent resistance of $290\ \Omega$ for the two parallel resistors in (a).



EXAMPLE 19–4 **Circuit with series and parallel.** How much current is drawn from the battery shown in Fig. 19–8a?

APPROACH The current I that flows out of the battery all passes through the $400\text{-}\Omega$ resistor, but then it splits into I_1 and I_2 passing through the $500\text{-}\Omega$ and $700\text{-}\Omega$ resistors. The latter two resistors are in parallel with each other. We look for simplicity, something that we already know how to treat. So let's start by finding the equivalent resistance, R_p , of the parallel resistors, $500\ \Omega$ and $700\ \Omega$. Then we can consider this R_p to be in series with the $400\text{-}\Omega$ resistor.

SOLUTION The equivalent resistance, R_p , of the $500\text{-}\Omega$ and $700\text{-}\Omega$ resistors in parallel is given by

$$\frac{1}{R_p} = \frac{1}{500\ \Omega} + \frac{1}{700\ \Omega} = 0.0020\ \Omega^{-1} + 0.0014\ \Omega^{-1} = 0.0034\ \Omega^{-1}.$$

This is $1/R_p$, so we take the reciprocal to find R_p . It is a common mistake to forget to take this reciprocal. Notice that the units of reciprocal ohms, Ω^{-1} , are a reminder. Thus

$$R_p = \frac{1}{0.0034\ \Omega^{-1}} = 290\ \Omega.$$

This $290\ \Omega$ is the equivalent resistance of the two parallel resistors, and is in series with the $400\text{-}\Omega$ resistor as shown in the equivalent circuit of Fig. 19–8b. To find the total equivalent resistance R_{eq} , we add the $400\text{-}\Omega$ and $290\text{-}\Omega$ resistances together, since they are in series, and find

$$R_{\text{eq}} = 400\ \Omega + 290\ \Omega = 690\ \Omega.$$

The total current flowing from the battery is then

$$I = \frac{V}{R_{\text{eq}}} = \frac{12.0\ \text{V}}{690\ \Omega} = 0.0174\ \text{A} \approx 17\ \text{mA}.$$

NOTE This I is also the current flowing through the $400\text{-}\Omega$ resistor, but not through the $500\text{-}\Omega$ and $700\text{-}\Omega$ resistors (both currents are less—see the next Example).

NOTE Complex resistor circuits can often be analyzed in this way, considering the circuit as a combination of series and parallel resistances.

CAUTION
Remember to take the reciprocal