

connected to three 4-Ω resistors in series, the total resistance is 12 Ω and the current through the entire circuit will be only 1 A.

Another simple way to connect resistors is in **parallel**, so that the current from the source splits into separate branches or paths, as shown in Fig. 19–4a. The wiring in houses and buildings is arranged so all electric devices are in parallel, as we already saw in Chapter 18, Fig. 18–20. With parallel wiring, if you disconnect one device (say, R_1 in Fig. 19–4a), the current to the other devices is not interrupted. Compare to a series circuit, where if one device (say, R_1 in Fig. 19–3a) is disconnected, the current *is* stopped to all the others.

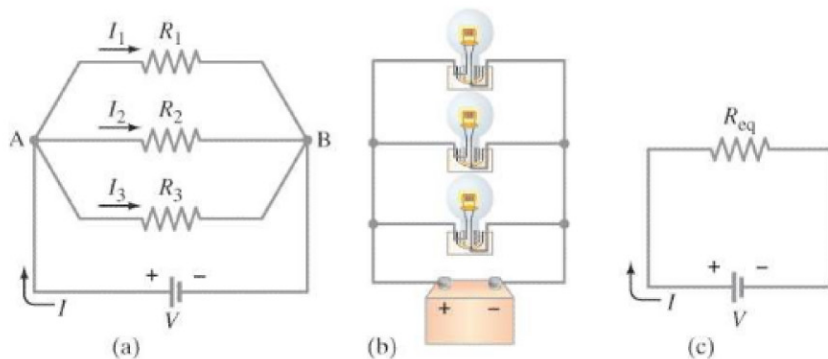


FIGURE 19–4
 (a) Resistances connected in parallel.
 (b) The resistances could be lightbulbs.
 (c) The equivalent circuit with R_{eq} obtained from Eq. 19–4:

$$\frac{1}{R_{\text{eq}}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}.$$

In a parallel circuit, Fig. 19–4a, the total current I that leaves the battery splits into three separate paths. We let I_1 , I_2 , and I_3 be the currents through each of the resistors, R_1 , R_2 , and R_3 , respectively. Because *electric charge is conserved*, the current I flowing into junction A (where the different wires or conductors meet, Fig. 19–4a) must equal the current flowing out of the junction. Thus

$$I = I_1 + I_2 + I_3. \quad \text{[parallel]}$$

When resistors are connected in parallel, each has the same voltage across it. (Indeed, any two points in a circuit connected by a wire of negligible resistance are at the same potential.) Hence the full voltage of the battery is applied to each resistor in Fig. 19–4a. Applying Ohm’s law to each resistor, we have

$$I_1 = \frac{V}{R_1}, \quad I_2 = \frac{V}{R_2}, \quad \text{and} \quad I_3 = \frac{V}{R_3}.$$

Let us now determine what single resistor R_{eq} (Fig. 19–4c) will draw the same current I as these three resistances in parallel. This equivalent resistance R_{eq} must satisfy Ohm’s law too:

$$I = \frac{V}{R_{\text{eq}}}.$$

We now combine the equations above:

$$\begin{aligned} I &= I_1 + I_2 + I_3, \\ \frac{V}{R_{\text{eq}}} &= \frac{V}{R_1} + \frac{V}{R_2} + \frac{V}{R_3}. \end{aligned}$$

When we divide out the V from each term, we have

$$\frac{1}{R_{\text{eq}}} = \frac{1}{R_1} + \frac{1}{R_2} + \frac{1}{R_3}. \quad \text{[parallel]} \quad \mathbf{(19-4)} \quad \text{Resistances in parallel}$$

For example, suppose you connect two 4-Ω loudspeakers to a single set of output terminals of your stereo amplifier or receiver. (Ignore the other channel for a moment—our two speakers are both connected to the left channel, say.)

*Parallel circuit:
currents add;
voltage the same across each R*