



FIGURE 17-10 Example 17-6.
(See also Example 16-9, Fig. 16-28.)

CAUTION
Potential is a scalar and has no components

EXAMPLE 17-6 **Potential above two charges.** Calculate the electric potential (a) at point A in Fig. 17-10 due to the two charges shown, and (b) at point B. [This is the same situation as Example 16-9, Fig. 16-28, where we calculated the electric field at these points.]

APPROACH The total potential at point A (or at point B) is the sum of the potentials at that point due to each of the two charges Q_1 and Q_2 . The potential due to each single charge is given by Eq. 17-5. We do not have to worry about directions because electric potential is a scalar quantity. But we do have to keep track of the signs of charges.

SOLUTION (a) We add the potentials at point A due to the each charge Q_1 and Q_2 , and we use Eq. 17-5 for each:

$$\begin{aligned} V_A &= V_{A2} + V_{A1} \\ &= k \frac{Q_2}{r_{2A}} + k \frac{Q_1}{r_{1A}} \end{aligned}$$

where $r_{1A} = 60 \text{ cm}$ and $r_{2A} = 30 \text{ cm}$. Then

$$\begin{aligned} V_A &= \frac{(9.0 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2)(5.0 \times 10^{-5} \text{ C})}{0.30 \text{ m}} \\ &\quad + \frac{(9.0 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2)(-5.0 \times 10^{-5} \text{ C})}{0.60 \text{ m}} \\ &= 1.50 \times 10^6 \text{ V} - 0.75 \times 10^6 \text{ V} \\ &= 7.5 \times 10^5 \text{ V}. \end{aligned}$$

(b) At point B, $r_{1B} = r_{2B} = 0.40 \text{ m}$, so

$$\begin{aligned} V_B &= V_{B2} + V_{B1} \\ &= \frac{(9.0 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2)(5.0 \times 10^{-5} \text{ C})}{0.40 \text{ m}} \\ &\quad + \frac{(9.0 \times 10^9 \text{ N} \cdot \text{m}^2/\text{C}^2)(-5.0 \times 10^{-5} \text{ C})}{0.40 \text{ m}} \\ &= 0 \text{ V}. \end{aligned}$$

NOTE The two terms in the sum in (b) cancel for any point equidistant from Q_1 and Q_2 ($r_{1B} = r_{2B}$). Thus the potential will be zero everywhere on the plane equidistant between the two charges. This plane is an equipotential surface with $V = 0$.

Simple summations like these can easily be performed for any number of point charges.