

For a given quantity of gas it is found experimentally that, to a good approximation, *the volume of a gas is inversely proportional to the absolute pressure applied to it when the temperature is kept constant.* That is,

$$V \propto \frac{1}{P}, \quad [\text{constant } T]$$

where P is the absolute pressure (*not* “gauge pressure”—see Section 10–4). For example, if the pressure on a gas is doubled, the volume is reduced to half its original volume. This relation is known as **Boyle’s law**, after Robert Boyle (1627–1691), who first stated it on the basis of his own experiments. A graph of P vs. V for a fixed temperature is shown in Fig. 13–12. Boyle’s law can also be written

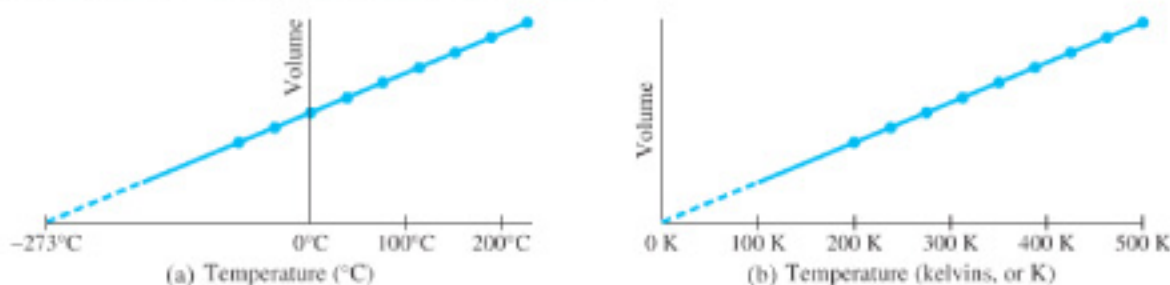
$$PV = \text{constant}. \quad [\text{constant } T]$$

That is, at constant temperature, if either the pressure or volume of the gas is allowed to vary, the other variable also changes so that the product PV remains constant.

Temperature also affects the volume of a gas, but a quantitative relationship between V and T was not found until more than a century after Boyle’s work. The Frenchman Jacques Charles (1746–1823) found that when the pressure is not too high and is kept constant, the volume of a gas increases with temperature at a nearly constant rate, as in Fig. 13–13a. However, all gases liquefy at low temperatures (for example, oxygen liquefies at -183°C), so the graph cannot be extended below the liquefaction point. Nonetheless, the graph is essentially a straight line and if projected to lower temperatures, as shown by the dashed line, it crosses the axis at about -273°C .

Such a graph can be drawn for any gas, and the straight line always projects back to -273°C at zero volume. This seems to imply that if a gas could be cooled to -273°C , it would have zero volume, and at lower temperatures a negative volume, which makes no sense. It could be argued that -273°C is the lowest temperature possible; indeed, many other more recent experiments indicate that this is so. This temperature is called the **absolute zero** of temperature. Its value has been determined to be -273.15°C .

FIGURE 13–13 Volume of a fixed amount of gas as a function of (a) Celsius temperature, and (b) Kelvin temperature, when the pressure is kept constant.



Absolute zero forms the basis of a temperature scale known as the **absolute scale** or **Kelvin scale**, and it is used extensively in scientific work. On this scale the temperature is specified as degrees Kelvin or, preferably, simply as *kelvins* (K) without the degree sign. The intervals are the same as for the Celsius scale, but the zero on this scale (0 K) is chosen as absolute zero. Thus the freezing point of water (0°C) is 273.15 K, and the boiling point of water is 373.15 K. Indeed, any temperature on the Celsius scale can be changed to kelvins by adding 273.15 to it:

$$T(\text{K}) = T(^{\circ}\text{C}) + 273.15.$$

Now let us look at Fig. 13–13b, where the graph of the volume of a gas versus absolute temperature is a straight line that passes through the origin. Thus, to a

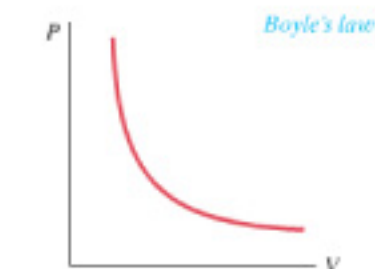


FIGURE 13–12 Pressure vs. volume of a fixed amount of gas at a constant temperature, showing the inverse relationship as given by Boyle’s law: as the pressure decreases, the volume increases.

Absolute zero

Kelvin scale

Conversion between Kelvin (absolute) and Celsius scales