

FIGURE 6-10 Example 6-6.

CONCEPTUAL EXAMPLE 6-6 Work to stop a car. A car traveling 60 km/h can brake to a stop within a distance d of 20 m (Fig. 6-10a). If the car is going twice as fast, 120 km/h, what is its stopping distance (Fig. 6-10b)? Assume the maximum braking force is approximately independent of speed.

**RESPONSE** Since the stopping force F is approximately constant, the work needed to stop the car, Fd, is proportional to the distance traveled. We apply the work-energy principle, noting that  $\vec{\mathbf{F}}$  and  $\vec{\mathbf{d}}$  are in opposite directions and that the final speed of the car is zero:

Then

$$W_{\text{net}} = Fd \cos 180^{\circ} = -Fd.$$
  
 $-Fd = \Delta_{\text{KE}} = \frac{1}{2}mv_2^2 - \frac{1}{2}mv_1^2$   
 $= 0 - \frac{1}{2}mv_1^2.$ 

Thus, since the force and mass are constant, we see that the stopping distance, d, increases with the square of the speed:

$$d \propto v^2$$
.

If the car's initial speed is doubled, the stopping distance is  $(2)^2 = 4$  times as great, or 80 m.

**EXERCISE B** Can kinetic energy ever be negative?

## 4 Potential Energy

Potential energy

We have just discussed how an object is said to have energy by virtue of its motion, which we call kinetic energy. But it is also possible to have potential energy, which is the energy associated with forces that depend on the position or configuration of an object (or objects) relative to the surroundings. Various types of potential energy (PE) can be defined, and each type is associated with a particular force.

The spring of a wind-up toy is an example of an object with potential energy. The spring acquired its potential energy because work was done on it by the person winding the toy. As the spring unwinds, it exerts a force and does work to make the toy move.

Gravitational PE

Perhaps the most common example of potential energy is gravitational potential energy. A heavy brick held high in the air has potential energy because of its position relative to the Earth. The raised brick has the ability to do work, for if it is released, it will fall to the ground due to the gravitational force, and can do work on, say, a stake, driving it into the ground. Let us seek the form for the gravitational potential energy of an object near the surface of the Earth. For an object of mass m to be lifted vertically, an upward force at least equal to its weight, mg, must be exerted on it, say by a person's hand.

Car's stopping distance \( \infty initial speed squared