

### CONCEPTUAL EXAMPLE 6-3 Does the Earth do work on the Moon?

The Moon revolves around the Earth in a nearly circular orbit, kept there by the gravitational force exerted by the Earth. Does gravity do (a) positive work, (b) negative work, or (c) no work on the Moon?

**RESPONSE** The gravitational force exerted by the Earth on the Moon (Fig. 6-5) acts toward the Earth and provides its centripetal acceleration, inward along the radius of the Moon's orbit. The Moon's displacement at any moment is tangent to the circle, in the direction of its velocity, perpendicular to the radius and perpendicular to the force of gravity. Hence the angle  $\theta$  between the force  $\vec{F}_G$  and the instantaneous displacement of the Moon is  $90^\circ$ , and the work done by the Earth's gravity on the Moon as it orbits is therefore zero ( $\cos 90^\circ = 0$ ). This is why the Moon, as well as artificial satellites, can stay in orbit without expenditure of fuel: no net work needs to be done against the force of gravity.

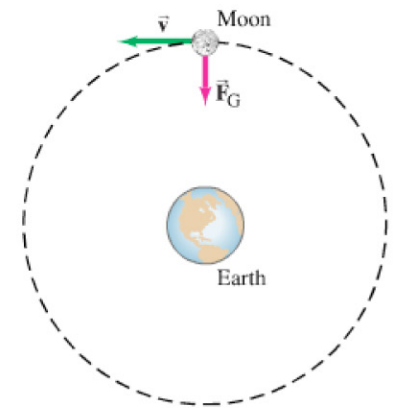


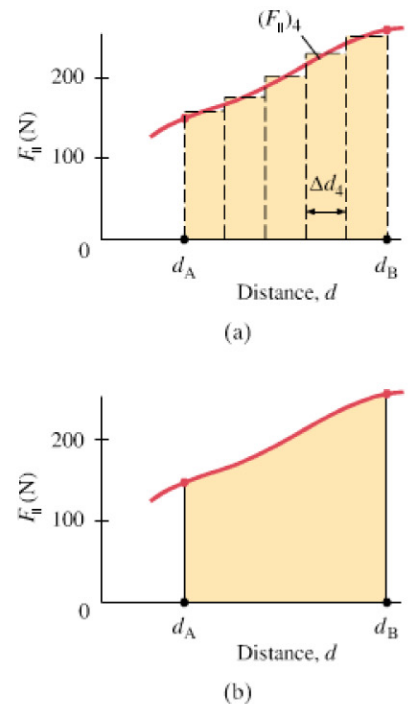
FIGURE 6-5 Example 6-3.

## \* 6-2 Work Done by a Varying Force

If the force acting on an object is constant, the work done by that force can be calculated using Eq. 6-1. But in many cases, the force varies in magnitude or direction during a process. For example, as a rocket moves away from Earth, work is done to overcome the force of gravity, which varies as the inverse square of the distance from the Earth's center. Other examples are the force exerted by a spring, which increases with the amount of stretch, or the work done by a varying force in pulling a box or cart up an uneven hill.

The work done by a varying force can be determined graphically. The procedure is like that for determining displacement when the velocity is known as a function of time (Section 2-8). To determine the work done by a variable force, we plot  $F_{\parallel}$  ( $= F \cos \theta$ , the component of  $\vec{F}$  parallel to the direction of motion at any point) as a function of distance  $d$ , as in Fig. 6-6a. We divide the distance into small segments  $\Delta d$ . For each segment, we indicate the average of  $F_{\parallel}$  by a horizontal dashed line. Then the work done for each segment is  $\Delta W = F_{\parallel} \Delta d$ , which is the area of a rectangle  $\Delta d$  wide and  $F_{\parallel}$  high. The total work done to move the object a total distance  $d = d_B - d_A$  is the sum of the areas of the rectangles (five in the case shown in Fig. 6-6a). Usually, the average value of  $F_{\parallel}$  for each segment must be estimated, and a reasonable approximation of the work done can then be made. If we subdivide the distance into many more segments,  $\Delta d$  can be made smaller and our estimate of the work done would be more accurate. In the limit as  $\Delta d$  approaches zero, the total area of the many narrow rectangles approaches the area under the curve, Fig. 6-6b. That is, *the work done by a variable force in moving an object between two points is equal to the area under the  $F_{\parallel}$  vs.  $d$  curve between those two points.*

**FIGURE 6-6** The work done by a force  $F$  can be calculated by taking: (a) the sum of the areas of the rectangles; (b) the area under the curve of  $F_{\parallel}$  vs.  $d$ .



## 6-3 Kinetic Energy, and the Work-Energy Principle

*Energy* is one of the most important concepts in science. Yet we cannot give a simple general definition of energy in only a few words. Nonetheless, each specific type of energy can be defined fairly simply. In this Chapter, we define translational kinetic energy and some types of potential energy. In later Chapters, we will examine other types of energy, such as that related to heat (Chapters 14 and 15). The crucial aspect of all the types of energy is that the sum of all types, the *total energy*, is the same after any process as it was before: that is, the quantity “energy” is a conserved quantity.

For the purposes of this Chapter, we can define energy in the traditional way as “the ability to do work.” This simple definition is not very precise, nor is it really valid for all types of energy.<sup>†</sup> It is valid, however, for mechanical energy which we discuss in this Chapter, and it serves to underscore the fundamental

<sup>†</sup>Energy associated with heat is often not available to do work, as we will discuss in Chapter 15.