

weight is still  $mg$ . The objects seem weightless only because the elevator is in free fall, and there is no contact force to make us feel the weight.

The “weightlessness” experienced by people in a satellite orbit close to the Earth is the same apparent weightlessness experienced in a freely falling elevator. It may seem strange, at first, to think of a satellite as freely falling. But a satellite is indeed falling toward the Earth, as was shown in Fig. 5–25. The force of gravity causes it to “fall” out of its natural straight-line path. The acceleration of the satellite must be the acceleration due to gravity at that point, since the only force acting on it is gravity. Thus, although the force of gravity acts on objects within the satellite, the objects experience an apparent weightlessness because they, and the satellite, are all accelerating as in free fall.

Figure 5–27 shows some examples of “free fall,” or apparent weightlessness, experienced by people on Earth for brief moments.

A different situation occurs when a spacecraft is out in space far from the Earth, the Moon, and other attracting objects. The force of gravity due to the Earth and other heavenly bodies will then be quite small because of the distances involved, and people in such a spacecraft will experience real weightlessness.

## \* 5–9 Kepler’s Laws and Newton’s Synthesis

More than a half century before Newton proposed his three laws of motion and his law of universal gravitation, the German astronomer Johannes Kepler (1571–1630) had worked out a detailed description of the motion of the planets about the Sun: three empirical findings that we now refer to as **Kepler’s laws of planetary motion**. They are summarized as follows, with additional explanation in Figs. 5–28 and 5–29.

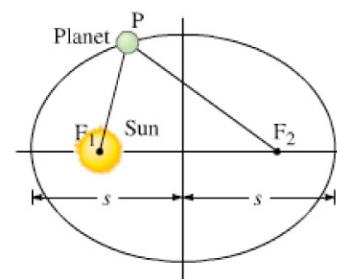
*Kepler’s first law:* The path of each planet about the Sun is an ellipse with the Sun at one focus (Fig. 5–28).

*Kepler’s second law:* Each planet moves so that an imaginary line drawn from the Sun to the planet sweeps out equal areas in equal periods of time (Fig. 5–29).

*Kepler’s third law:* The ratio of the squares of the periods  $T$  of any two planets revolving about the Sun is equal to the ratio of the cubes of their mean distances  $s$  from the Sun:  $(T_1/T_2)^2 = (s_1/s_2)^3$ . [Actually,  $s$  is the semimajor axis, defined as half the long (major) axis of the orbit, as shown in Fig. 5–28. We can also call it the mean distance of the planet from the Sun.] Present-day data are given in Table 5–2: see the last column.

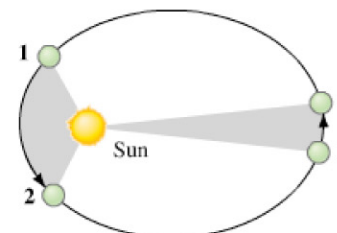
Kepler arrived at his laws through careful analysis of experimental data. Fifty years later, Newton was able to show that Kepler’s laws could be derived mathematically from the law of universal gravitation and the laws of motion. Newton also showed that for any reasonable form for the gravitational force law, only one that depends on the inverse square of the distance is fully consistent with Kepler’s laws. He thus used Kepler’s laws as evidence in favor of his law of universal gravitation, Eq. 5–4.

### “Weightlessness” in a satellite



**FIGURE 5–28** (a) *Kepler’s first law.* An ellipse is a closed curve such that the sum of the distances from any point  $P$  on the curve to two fixed points (called the foci,  $F_1$  and  $F_2$ ) remains constant. That is, the sum of the distances,  $F_1P + F_2P$ , is the same for all points on the curve. A circle is a special case of an ellipse in which the two foci coincide, at the center of the circle.

**FIGURE 5–29** *Kepler’s second law.* The two shaded regions have equal areas. The planet moves from point 1 to point 2 in the same time as it takes to move from point 3 to point 4. Planets move fastest in that part of their orbit where they are closest to the Sun. Exaggerated scale.



**TABLE 5–2 Planetary Data Applied to Kepler’s Third Law**

Planet	Mean Distance from Sun, $s$ ( $10^6$ km)	Period, $T$ (Earth years)	$s^3/T^2$ ( $10^{24}$ km <sup>3</sup> /y <sup>2</sup> )
Mercury	57.9	0.241	3.34
Venus	108.2	0.615	3.35
Earth	149.6	1.0	3.35
Mars	227.9	1.88	3.35
Jupiter	778.3	11.86	3.35
Saturn	1427	29.5	3.34
Uranus	2870	84.0	3.35
Neptune	4497	165	3.34
Pluto	5900	248	3.34